where $w(z)$ = width of the dam face (m) at elevation z (Fig. P17.9b). The line of action can also be obtained by evaluating

$$d = \frac{\int_0^D \rho g z w(z)(D-z)\,dz}{\int_0^D \rho g w(z)(D-z)\,dz}$$

Use Simpson's rule to compute f_t and d.

17.10 The force on a sailboat mast can be represented by the following function:

$$f(z) = 200\left(\frac{z}{7+z}\right)e^{-2.5z/H}$$

where z = the elevation above the deck and H = the height of the mast. The total force F exerted on the mast can be determined by integrating this function over the height of the mast:

$$F = \int_0^H f(z)\,dz$$

The line of action can also be determined by integration:

$$d = \frac{\int_0^H z f(z)\,dz}{\int_0^H f(z)\,dz}$$

(a) Use the composite trapezoidal rule to compute F and d for the case where $H = 30$ ($n = 6$).

(b) Repeat **(a)**, but use the composite Simpson's 1/3 rule.

17.11 A wind force distributed against the side of a skyscraper is measured as

Height l, m	0	30	60	90	120
Force, $F(l)$, N/m	0	340	1200	1600	2700
Height l, m	150	180	210	240	
Force, $F(l)$, N/m	3100	3200	3500	3800	

Compute the net force and the line of action due to this distributed wind.

17.12 An 11-m beam is subjected to a load, and the shear force follows the equation

$$V(x) = 5 + 0.25x^2$$

where V is the shear force, and x is length in distance along the beam. We know that $V = dM/dx$, and M is the bending moment. Integration yields the relationship

$$M = M_o + \int_0^x V\,dx$$

If M_o is zero and $x = 11$, calculate M using **(a)** analytical integration, **(b)** multiple-application trapezoidal rule, and **(c)** multiple-application Simpson's rules. For **(b)** and **(c)** use 1-m increments.

17.13 The total mass of a variable density rod is given by

$$m = \int_0^L \rho(x)A_c(x)\,dx$$

where m = mass, $\rho(x)$ = density, $A_c(x)$ = cross-sectional area, x = distance along the rod and L = the total length of the rod. The following data has been measured for a 10-m length rod. Determine the mass in grams to the best possible accuracy.

x, m	0	2	3	4	6	8	10
ρ, g/cm^3	4.00	3.95	3.89	3.80	3.60	3.41	3.30
A_c, cm^2	100	103	106	110	120	133	150

17.14 A transportation engineering study requires that you determine the number of cars that pass through an intersection traveling during morning rush hour. You stand at the side of the road and count the number of cars that pass every 4 minutes at several times as tabulated below. Use the best numerical method to determine **(a)** the total number of cars that pass between 7:30 and 9:15, and **(b)** the rate of cars going through the intersection per minute. (Hint: Be careful with units.)

Time (hr)	7:30	7:45	8:00	8:15	8:45	9:15
Rate (cars per 4 min)	18	24	14	24	21	9

17.15 Determine the average value for the data in Fig. P17.15. Perform the integral needed for the average in the order shown by the following equation:

$$I = \int_{x_0}^{x_n}\left[\int_{y_0}^{y_m} f(x,y)\,dy\right]dx$$

17.16 Integration provides a means to compute how much mass enters or leaves a reactor over a specified time period, as in

$$M = \int_{t_1}^{t_2} Qc\,dt$$

where t_1 and t_2 = the initial and final times, respectively. This formula makes intuitive sense if you recall the analogy between integration and summation. Thus, the integral represents the summation of the product of flow times concentration to give the total mass entering or leaving from t_1 to t_2.